EP155 February 6, 2006 Midterm #1

Name: SOLUTION Student No.	
Date: February 6, 2006 Time: 1 hour Restrictions: Calculators and one 8.5 by 11 sheet of paper only The sheet of paper can be written on both sides.	
Put a box around all your answers!	
Show the units!	
CONSTANTS: $k = 8.99 \times 10^9 \text{ N m}^2/\text{C}^2$ $\epsilon_o = 8.85 \times 10^{-12} \text{ C}^2/(\text{N m}^2)$ PREFIXES: μ is 10^{-6} m is 10^{-3} k is 10^3	

QUES.	MARKS
Q1 (6)	
Q2 (8)	
Q3 (6)	
Q4 (6)	
Total (26)	

(2) 1. (a) An object is moved from point (x,y)=(7 m, 49 m) to point (x,y)=(19 m, 9 m). The object is moved with a constant force vector

$$\vec{F} = (10\,\hat{i} - 7\,\hat{j}) \text{ N}.$$

How much work is done on the object by the force?

$$W = \vec{F} \cdot \vec{d}$$
; $\vec{d} = \text{fund position} - \text{civital position}$
 $\vec{d} = (19m, 9m) - (7m, 49m) = (12m, -40m)$
 $W = (10N, -7N) \cdot (12m, -40m)$
 $W = (10N)(12m) + (-7N)(-40m)$
 $W = 120J + 280J$
 $W = 400J$

(4) (b) An object is moved in a straight line from point A, which is located at (x,y) = (0 m, 0 m) to point B, which is located at (x,y)=(10 m, 0 m). It is then moved in another straight line from point B to point D, which is located at (x,y)=(10 m, 6 m). The object is moved with a constant force vector F. The force does 10 J of work to move the object from point A to point B and 12 J of work to move the object from point B to point D.

What is the force vector \vec{F} ?

Let $\vec{F} = F_{x} \hat{i} + F_{y} \hat{j}$ The dectance vector for moving from A to B is $\vec{d}_{i} = (10 \text{ m}, 0 \text{ m}) - (0 \text{ m}, 0 \text{ m}) = (10 \text{ m}, 0 \text{ m})$ The work done in moving the object from A to B is given by: $\vec{W} = \vec{F} \cdot \vec{d}_{1} = (F_{x}, F_{y}) \cdot (10 \text{ m}, 0 \text{ m})$. $\vec{V} = \vec{F} \cdot \vec{d}_{1} = (F_{x}, F_{y}) \cdot (10 \text{ m}, 0 \text{ m})$. $\vec{V} = \vec{F} \cdot \vec{d}_{1} = (F_{x}, F_{y}) \cdot (10 \text{ m}, 0 \text{ m})$. $\vec{V} = \vec{F} \cdot \vec{d}_{1} = (F_{x}, F_{y}) \cdot (10 \text{ m}, 0 \text{ m})$. $\vec{V} = \vec{F} \cdot \vec{d}_{1} = (F_{x})(10 \text{ m}) + (F_{y})(0 \text{ m})$.

The destance vector for moving from B to D is $\vec{d}_2 = (Dm, 6m) - (IOm, Om) = (Om, 6m)$ The work done in moving the object from B to D is $W = \vec{F} \cdot \vec{d}_2 = (F_x, F_y) \cdot (Om, 6m)$ $\vec{d}_2 = (F_x)(0) + (F_y)(6m)$

$$F_{y} = \frac{12J}{6m} = 2N$$

- 2. The field lines for an electric field are shown in Figure 1. There are several points shown on the field. It is known that the electric field strengths at points A, B and D are 10 N/C, 12 N/C and 14 N/C respectively.
- (2) (a) Draw an equipotential line (i.e., an energy contour line) through point A.
- (2) (b) The distance between points A and B is 7 m (the distance is measured along the field line that links them) and the distance between points B and D is 5 m (the distance is measured along the field line that links them).
 Approximately what is the electic potential at point A with respect to point D (i.e., Approximately what is V_{AD})?

VAD = W = pools required to move Q = from point D to point A.

First determine the arginal 40. If Q = positive the field will except a.

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First determine the arginal 40 move the first D to B.

When a work required to move Q = from D to B.

When a work required to move Q = from B to A.

When a company (d) = Eare d = (12+14 N) 5 m = 65 I = 65 V.

When a company (d) = Eare d = (10+12) N 7m = 77 I = 77 V.

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When a company (d) = Eare d = (10+12) N 7m = 77 I = 77 V.

When a company (d) = Eare d = (10+12) N 7m = 77 I = 65 V + 77 V = 142 V.

Q = (2) How much work is required to move +9 C of charge from point A to point D.

VDA = W work required to move Qt from A to D.

Pasitive charge so moved in derection of field line

Therefore the work will be negative

M = VDA Qt = -VADQt = (-142V)(9C) = -1278J

W = -1278J

(2) (d) Approximately what is V_{AG} ?

To find VAG draw a equipotential line through
point G to determine where it extensects the field
line That has point A, B, and C. Then calculate (roughly)
the work required to move Q+ from the entensection to
point A.

Was - Work & more Q+ from enhanced to point A.

VAG - Was Q+

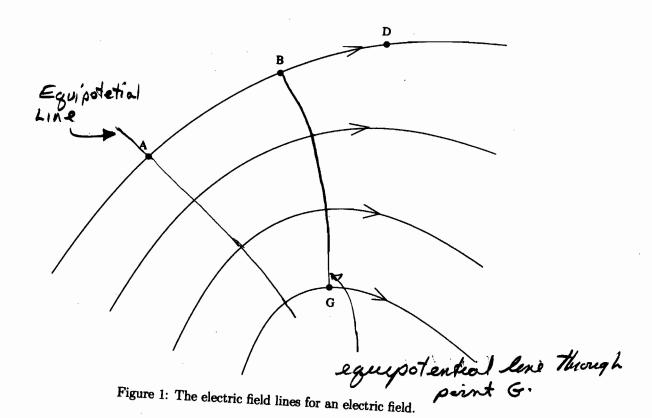
In drawing the equipotential line through purit 6, it is found that it untieseds the top feeler line at point B.

.. VAG = VAB = W = (Fave) (distance from B to A).

$$V_{AG} = \frac{10+12}{2} \frac{N}{c} (7m) = .77 V.$$

check the sign. The field force (on pas, twie Qz) is & the right and the charge is moved to the left: work done is possitive.

: VAG+ The checks



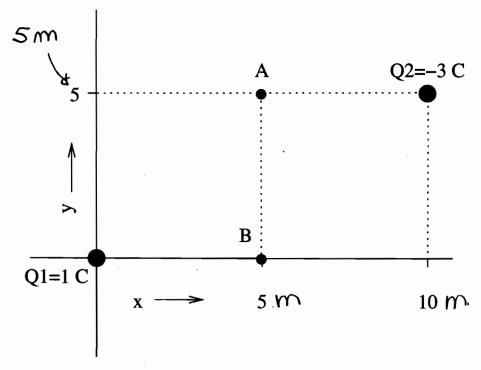


Figure 2: Position of point charges Q1 and Q2 as well as points A and B.

- 3. Two charge particles are positioned as shown in Figure 2. One particle is charged with Q1 = +1C and the other is charged with Q2 = -3C.
- (2) (a) If a test charge of $Q_t = +1$ C is placed at point A, what force would it experience due the field set up by point charges Q1 and Q2? The force will be a vector.

Let Fi = Fixî+Figî be the compenent of F due to change Qz and let Fiz = Fixî+Figî be the compenent of be the compenent of force due to Qz. We can get IFI and IFI using Coulombs law.

 $|\vec{F}_1|^2 \frac{|\vec{F}_1|^2}{|\vec{F}_2|^2} = \frac{|\vec{F}_1|^2 \sqrt{|\vec{F}_2|^2}}{|\vec{F}_1|^2} = \frac{|\vec{F}_1|^2 \sqrt{|\vec{F}_1|^2}}{|\vec{F}_1|^2} = \frac{|\vec{F}_1|^2}{|\vec{F}_1|^2} = \frac{|$

$$|\vec{F_2}| = \frac{k Q_2 Q_E}{r_2^2} = \frac{(8.99 \times 10^9 \text{Nm}^2)(3c)(1)}{(5m)^2} = 1.079 \times 10^9 \text{N}$$

Since Q1 & Q+ are both pasitive, the force due to Q1 is repulsive. From the geometry Fix = Fig and both are positive.

:. Fix = Fig = |Fi| = 0.180 × 109 = 0.127 × 109 N

Sanie Q2 Q sue of opposite signing the free wone of athaction of is.

F2 2 |F2| i z 1.079 × 10 N i

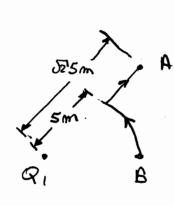
F=F1+F2=1.206 XION i+0.127X10 Nj

(b) What is V_{AB} ?

VAR 2 W & work done in moving Q from point 8 & point A.

It is easiest to find W in two otess. Find the work done to oversome the force due to Q, and the find the work done to overceme the force due to Oz and finally, sum the results. to get W.

First find to work done to overcome the force sue to Q1. Meed to choose a sensible path, which is one that either follows an equipotential line or a f 'a line. The path: Start at point B, move counter clockwise account. a semicircle with conten at Q1 until the field line that goes through point A is reached. Then follow the field. line to point B.



No work is done white moving on the service as the path is perpendicular to the feeld lines.

The worke done to morning Q+ (if Q+ is positive) along the feeld line is megative as the field wodorng the work. The magnitude of the work done is

|W1 = (8.99×109 Nm²)(1C) QE | I - I = 0.527×10 Nm |PE |. W1 = - 0.527X109 VQ

For work required to overcome force due to Q2 use patt.

|W2 | = 8.99 × 109 Nm2 (3C) (92) | 1 - 1 |

/W2 = 1.580 ×10 VQ+. work dono is negative of the so positive serie azid neg.

Wz = -1.58 x109 VQt.

4. A parallel plate capacitor has the following attributes.

The area of each plate is 0.15 m².

The distance between the plates is 10^{-5} m.

The material between the plates is polystyrene (Polystyrene has a dielectric constant of 2.6.).

The voltage across the plates is 10 V.

(2) (a) What is the capacitance of the capacitor?

$$C = \frac{1060 \, \text{A}}{\text{a}} = \frac{(2.6)(8.85 \times 10^{-12} \, \text{c}^2)}{\text{m}^2 \, \text{N}} = \frac{(0.15 \, \text{m}^2)}{10^{-5} \, \text{m}}$$

$$C = 0.345 \, \text{N} = \frac{(0.345 \, \text{M})^{-6} \, \text{c}^2}{\text{N} \, \text{m}}$$

(2) (b) What is the amount of charge (excess charge) on each plate of the capacitor?

(2) (c) What is the electric field strength between the plates of the capacitor?

full attrength, which is constant between the plates

V = E d. distance between plate:

Luoltage aeroso the plates
$$E = \frac{V}{d} = \frac{10V}{10^{-5}m} = \frac{10^{6} V}{m} = \frac{10^{6} N}{c}$$

Othernate method. $E = \frac{V_{off}}{E_0} = \frac{|Q_{off}|}{E_0 A} = \frac{|Q_{off}|}{E_0 A} = \frac{V_{off}}{E_0 A} = \frac{V_{off}}{E_0 A}$

which results in some formula

James Mustakos Question 1a) The most common mistake was taking the dot product incorrectly and getting a vector result. Work is a scales and a dot product results en a scale. W = F. d = (10,-7) - (12, -40) = (10)(12) + (-7)(-40) = 120 + 280 W = 400) NOTE: (10, -7) · (12, -4) # 120 c + 280;

Question 26 In defferent mistakes were aften. made in computing the average force. The first was the colcelation of average force on charge Que when it is moved from sount B & sount A. W 4 Fave d ; Face = FB + FA Fave # Fo - Fn The second commonly made mistake was using a less accleste average force in computing the work on moving charge. Q+ from point D to point A
work to move from D to B. = W, + W2 & work to move for & ton. $\frac{2}{5}\left(\frac{F_{1}+F_{2}}{2}\right) + \left(\frac{F_{1}+F_{2}}{2}\right) + \frac{2}{5}\left(\frac{F_{1}+F_{2}}{2}\right) + \frac{2}{$ Using average force Foton and destance 12 m yell a less accusé result W= 6Fo+6Fo

Decastion 36) The most common mustake was find the overage force encorrect by and then use this average force to find the work done. Noto that if F(r) = K9, Qe Then the average orce applied from T= 12 to T= 14 Tory + For the average force es en fact. Karat atr FS AVE = L Fs Ave = W = Es ave (r) d Fg-10. W = KO, Q. [1 -1] NOTE: You were guen the formula for work and cled not need to find Frage

Question 40 Several students used the formula for the energy stored in a capacitor to compute the electric field strongth. Perhaps they used the letter E to represent both electric field strangth and energy so had two formula's on their object that confidenced E and secked the wrong one in the heat of the battle. I am just quessing that this may be the case.